

# Experimental study on dead water resistance of a barge in a two-layer fluid

---

**Ying Gou, Xinwei Zhang, Bin Teng**

***State Key Laboratory of Coastal and Offshore Engineering  
Dalian University of Technology***

***International Academic Research Exchange Workshop on Ship and Ocean Engineering, Osaka, January 20, 2018***

# Motivation

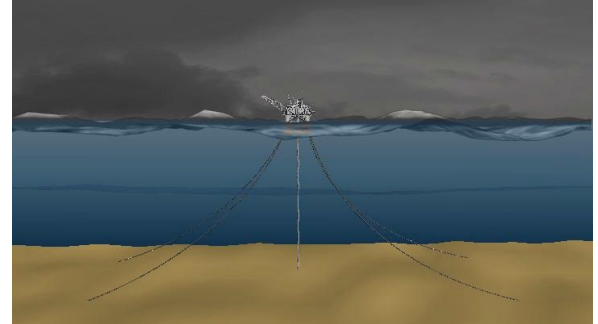
- In order to simulate drift motion of the deep sea platform, the drift damping is introduced. Drift damping can be obtained approximately by towing behavior with low speed.

$$F_d^{(2)}(\omega, U) = F_d^{(2)}(\omega, 0) + U \frac{\partial F_d^{(2)}}{\partial U} + O(U^2)$$

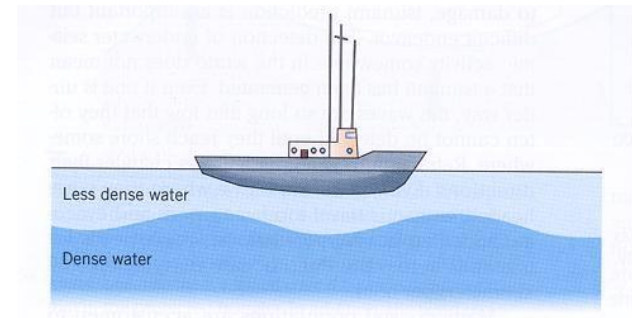
$B(\omega)$

- Density stratification is common in real ocean. ‘**Dead water**’ is possible phenomenon when the boat sailing on the stratified ocean.

**Dead water:** comes from the increased resistance that boats experience in stratified fluid. (Nansen’s observation, 1893)



**Platform in deep water**



# Motivation

---

- Flow of ice and the towing operation of barge could be affected by the ocean stratification.



**Flow of ice floe**



**Platform with towing operation**

# Outline

---

## 1. Background

- 1.1 Research progress
- 1.2 Objective of present study

## 2. Experimental setup

- 2.1 Experimental layout
- 2.2 Measurement method
- 2.3 Experiment parameters

## 3. Results and discussions

- 3.1 Drag resistance in uniform fluid
- 3.2 Drag resistance in a two-layer fluid
- 3.3 Dead water resistance coefficient in a two-layer fluid
- 3.4 Pycnocline elevation

## 4. Conclusions

---

# 1. Background

# 1. Background

## 1.1 Research progress

### ■ Ekman (1904)

On dead water, Ph.D Thesis

### ■ Hudimac (1961)

Ship waves in a stratified ocean. *J. Fluids Mechanics*

Asymptotic expansion method. A thin ship.

### ■ Miloh, Tulin, Zilman. (1993)

Dead-water effects of a ship moving in stratified seas. *Journal of Offshore Mechanics and Arctic Engineering*

Boundary integral equation

Slender body: prolate spheroid

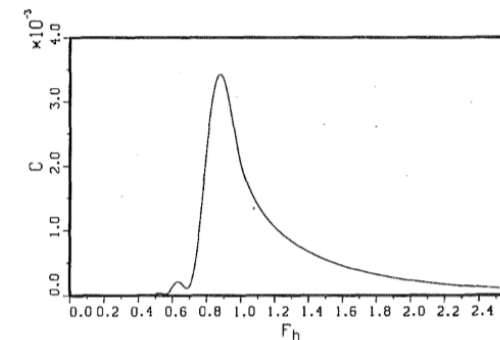
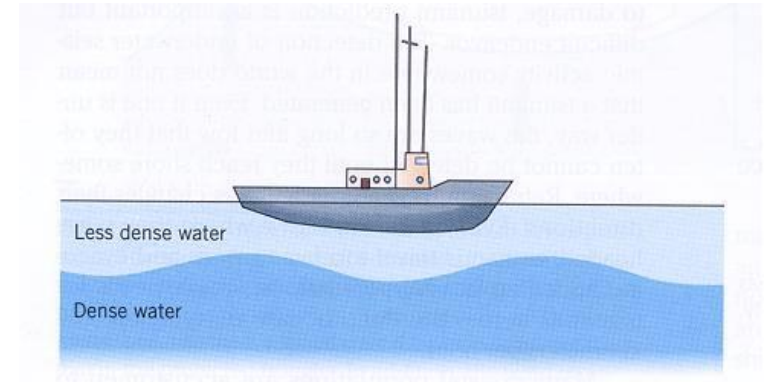


Fig. 1 Wave resistance coefficient  $C = 4R_w/\rho U^2 DL$  of a prolate-spheroid of length  $L$  and maximum diameter  $D$  moving on the free-surface of a two-layer fluid:  $h_1 = h$ ,  $h_2 \rightarrow \infty$ ,  $D/h = 0.9$ ,  $L/h = 10.0$

# 1. Background

## 1.1 Research progress

- Linton and McIver (1995)

- Cadby and Linton (2000)

Multipole expansions method

- Yeung and Nguyen (1999)

Waves generated by a moving source in a two-layer ocean of finite depth.

*J. Eng. Math.*

Green Function

Scattering of floating structure

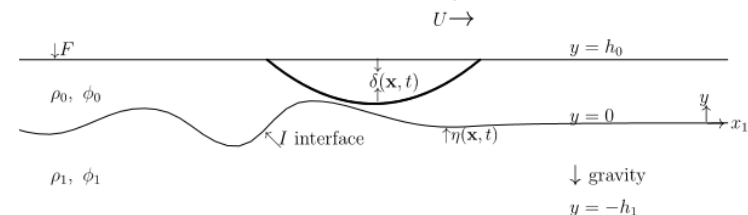
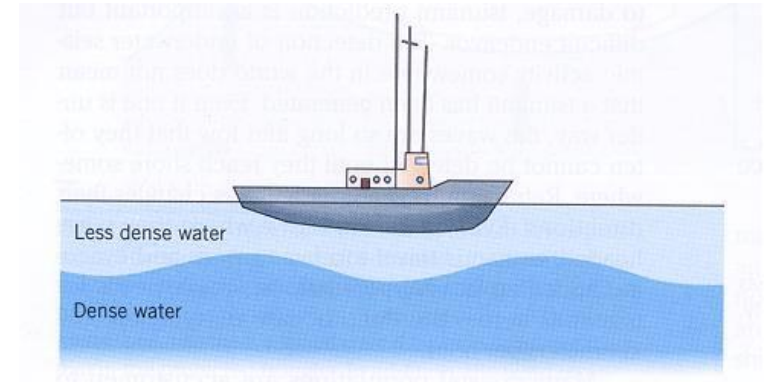
- Grue (2015).

Nonlinear dead water resistance at subcritical speed. *Physics of Fluids*.

Fourier translation method

Nonlinear theory

Ship geometry



# 1. Background

## 1.1 Research progress

- Mercier, Vasseur, and Dauxois, (2011).

Resurrecting dead-water phenomenon. **Wave flume:  $L=3.0\text{m}$ ,  $W=0.105\text{m}$ ,  $D=0.5\text{m}$**   
*Nonlinear Processes in Geophysics*

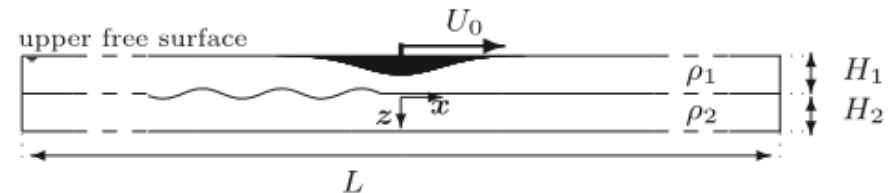
2D experiment; Steady force

- Lacaze et al., 2013.

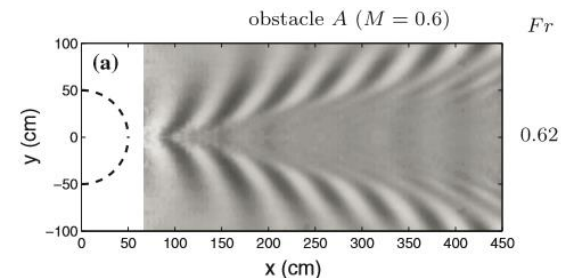
Wave patterns generated by an axisymmetric obstacle in a two-layer flow.

*Experiments in Fluids*

3D experiment; Focus on the wave wake



**Fig. 1** Sketch of the experimental set-up ( $L = 22\text{ m}$  and  $H_1 \approx H_2 \approx 15\text{ cm}$ )





# 1. Background

## 1.1 Research progress

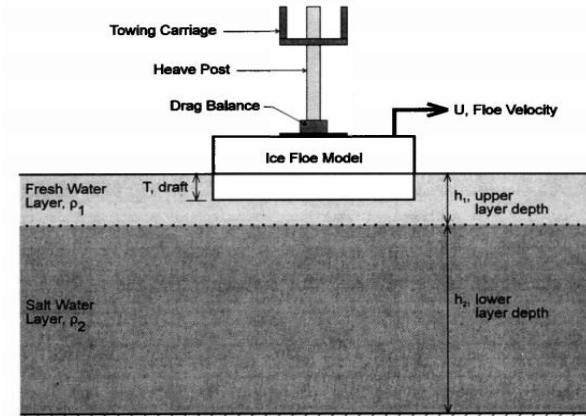
■ J. K. Waters, M.S. Bruno (1995).

Internal wave generation by ice floes moving in stratified water: Results from a laboratory study.

*Journal of Geophysical Research*

3D experiment;

Focus on the effect of ice profile on resistance



Wave flume:  $W=3.6\text{m}$

Ice flow:  $0.91\text{m} \times 0.91\text{m} \times 0.3\text{m}$

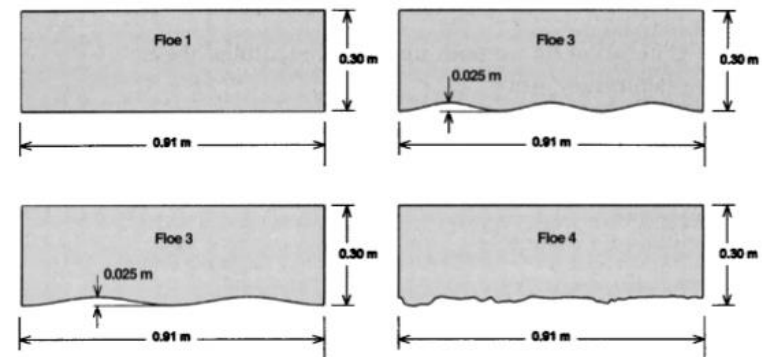


Figure 1. Profile views of model ice floes.

# 1. Background

---

## 1.2 Objective of present study

- This experiment study is to investigate the dead water resistance on box-type structure in a two-layer fluid.
- The draft and towing speed are varied to achieve the informations on the corresponding trends.



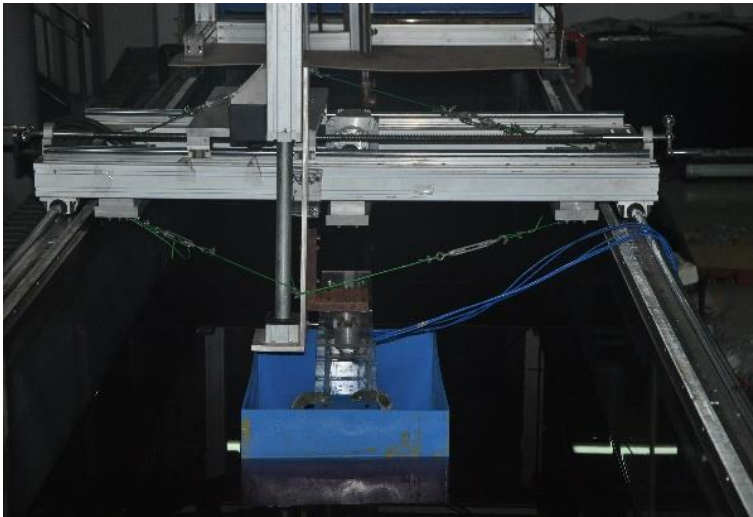
Arctic iceberg. Image: Florida State University

---

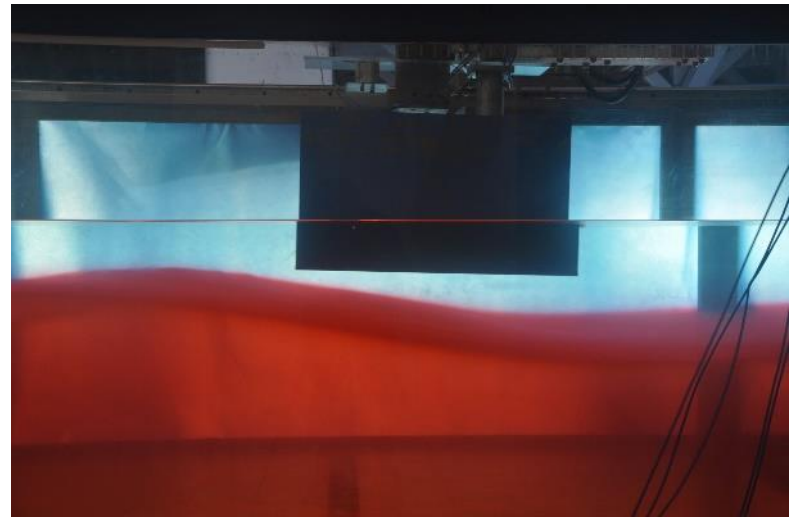
## **2. Experimental setup**

# 2.1 Experimental layout

- Wave flume:  $L=12.0\text{m}$ ,  $B=1.2\text{m}$ ,  $H=0.6\text{m}$
- Barge model:  $l=0.6\text{m}$ ,  $b=0.45\text{m}$



Front end view



Side view

The flume is equipped with a low speed towing system.

The fresh water with depth  $h_1$  is layered above the colored saline water with depth  $h_2$

## 2.2 Measurement method

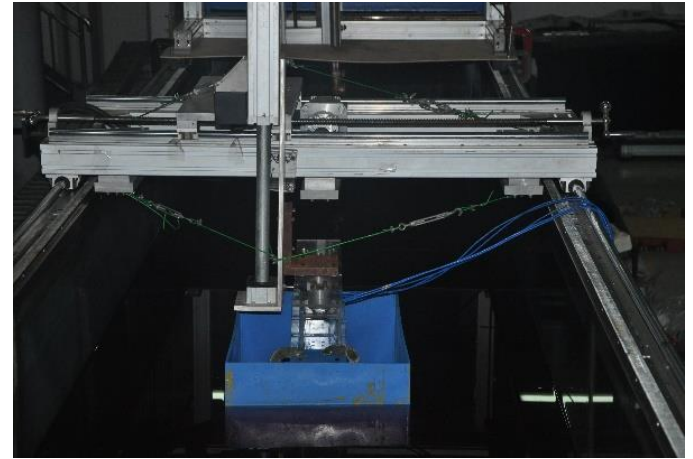
- Force sensor is use to measure the drag resistance. Sample frequency is in the range of 120HZ~480HZ
- Force sensor connected the model to the towing system with an aluminum alloy column
- The resistance values were obtained by averaging the data over the steady stage with stable towing speed.

$$\bar{f} = \frac{\sum_{i=1}^N f_i}{N}$$

- The equation of drag resistance is:

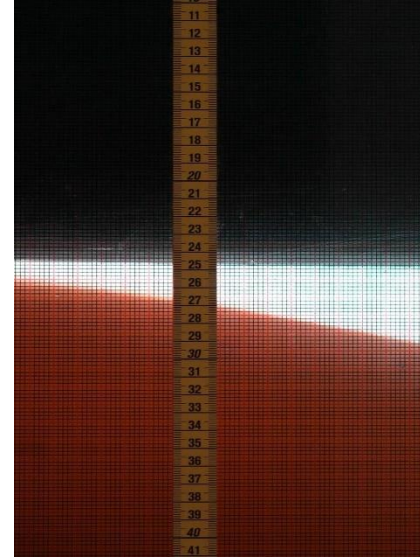
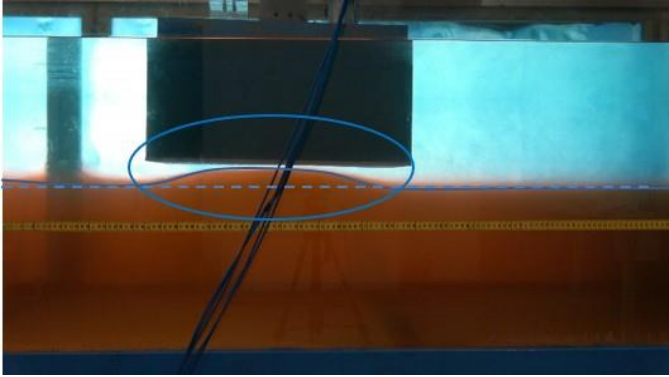
$$F = \frac{1}{2} C S \rho V^2$$

$$C_d = C_{two-layer} - C_{uniform}$$



## 2.2 Measurement method

---



- Pycnocline elevation is measured by camera and ruler.

## 2.3 Experimental parameters

### Test in two-layer fluid

| Interfacial position                   | Barge draft (m) | Towing speed (m/s)   |
|--|-----------------|--|
| $h_1=0.2\text{m}$<br>$h_2=0.4\text{m}$ | 0.10            | 0.06; 0.08; 0.10;<br>0.12; 0.14; 0.16;<br>0.18; 0.20; 0.24 |
|  | 0.12            |  |
|  | 0.14            |  |
|  | 0.20            |  |
| $h_1=0.3\text{m}$<br>$h_2=0.3\text{m}$ | 0.20            |  |
|  | 0.22            |  |
|  | 0.24            |  |

$$\rho_1=0.997\text{g/cm}^3, \quad \rho_2=1.025\text{g/cm}^3, \quad \rho_1/\rho_2=0.973$$

### Test in uniform fluid

| Water depth     | Barge draft                           | Towing speed (m/s)                                      |
|-----------------|---------------------------------------|---|
| $h=0.6\text{m}$ | 0.10, 0.12, 0.14, 0.20, 0.22,<br>0.24 | 0.06; 0.08; 0.10; 0.12; 0.14;<br>0.16; 0.18; 0.20; 0.24 |

---

## **3. Results and discussions**



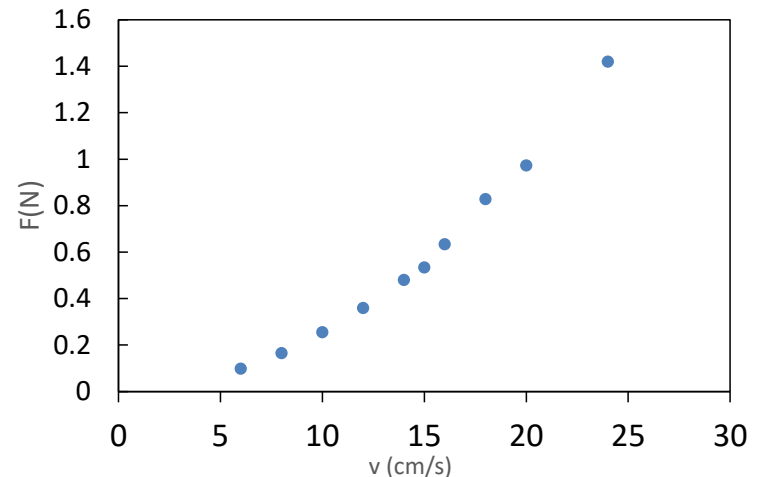
# 3.1 Drag force in uniform fluid

- ◆ The resistance is directly proportional to the square of the towing velocity  $V$ .
- ◆ That means the drag resistance coefficient  $C_{\text{uniform}}$  = constant with a certain draft

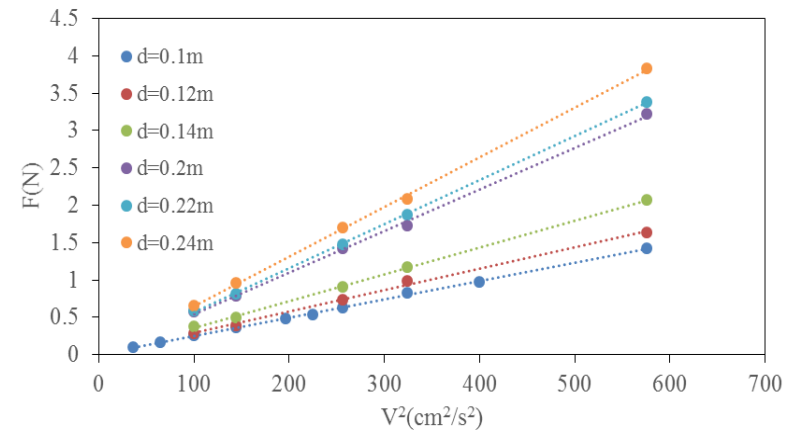
$$F = \frac{1}{2} CS \rho V^2$$

$$F = F_{\text{friction}} + \underline{F_{\text{form drag}}} + F_{\text{wave-making}}$$

$$0.025 < Fr = \frac{V}{\sqrt{gL}} < 0.099$$



Drag force vs.  $V$ ,  $d=0.1\text{m}$

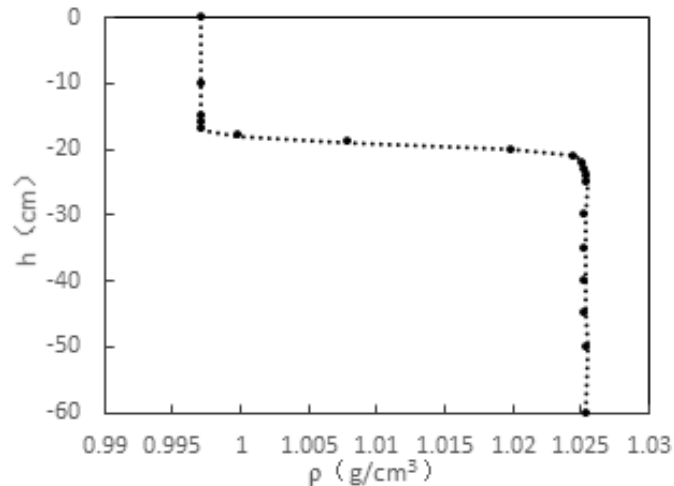


Drag force vs.  $V^2$

## 3.2 Drag force in a two-layer fluid

### ➤ Density profile before towing tests

Pycnocline thickness is about 0.05m before the towing test

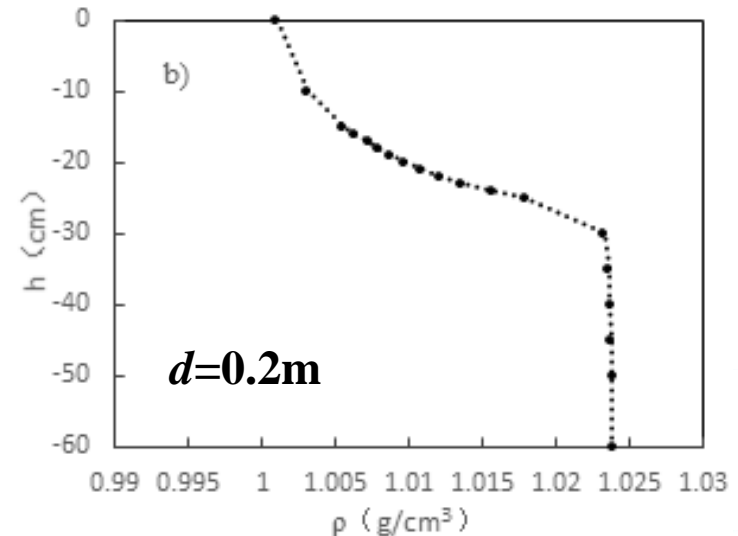
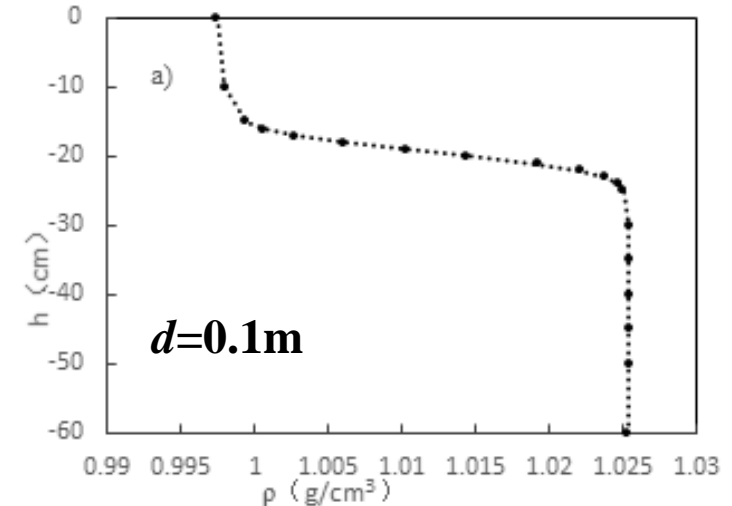


$$h_1 = 0.2\text{m}, \quad \rho_1 = 0.997\text{g/cm}^3$$

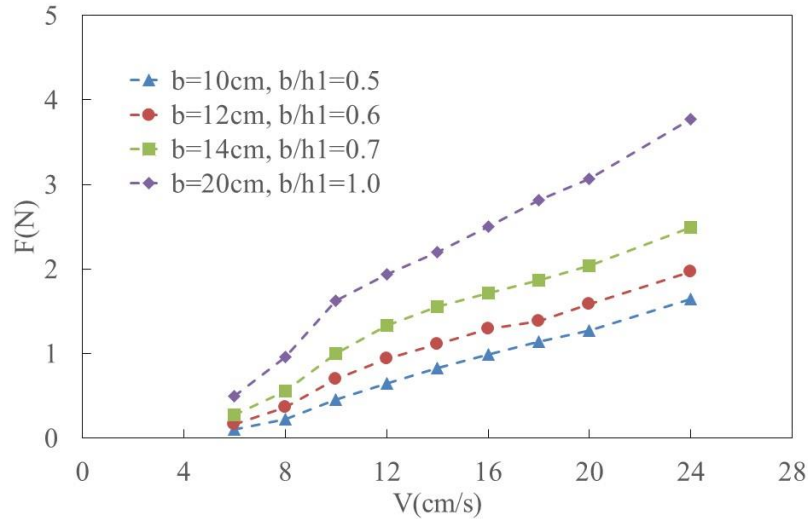
$$h_2 = 0.4\text{m}, \quad \rho_2 = 1.025\text{g/cm}^3$$

$$\rho_1/\rho_2 = 0.973$$

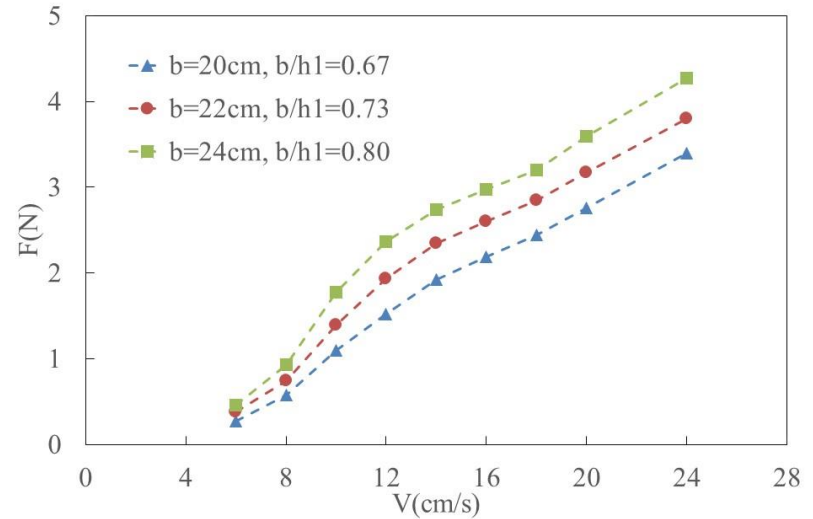
### ➤ Density profile after towing tests



## 3.2 Drag force in a two-layer fluid



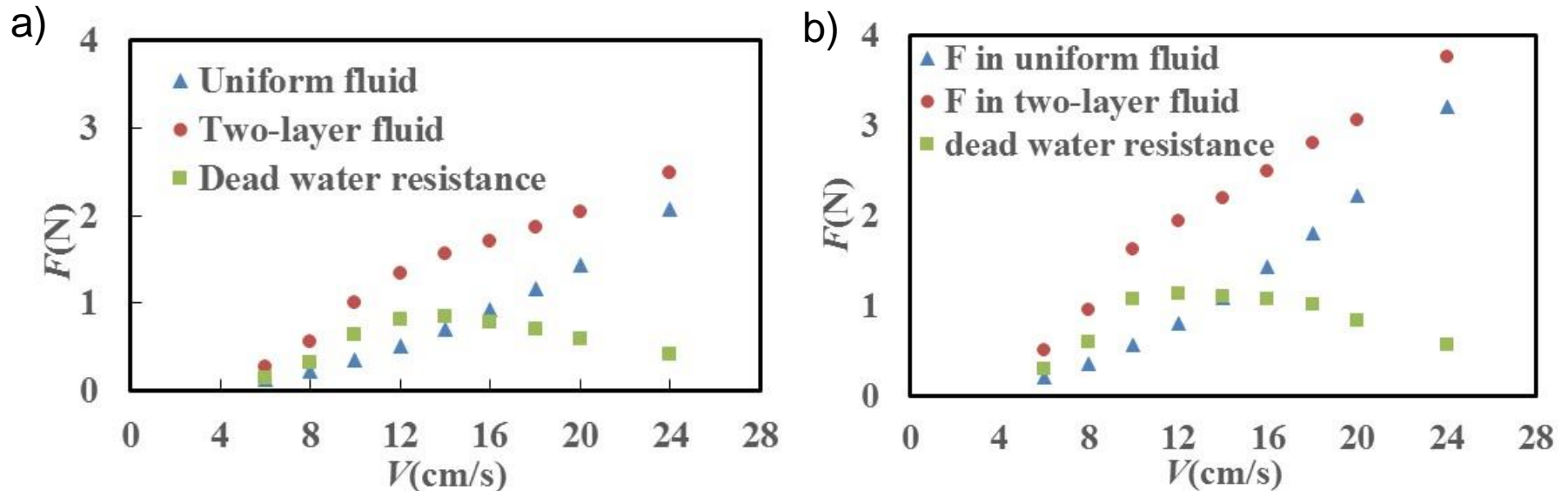
(a)  $h_1=0.2m, h_2=0.4m$



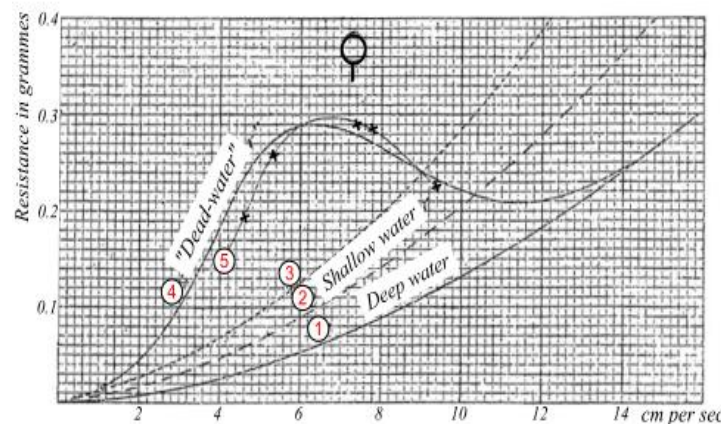
(b)  $h_1=0.3m, h_2=0.3m$

- ◆ **Shallow draft: the drag resistance increases approximate linearly with the increase of the towing speed**
- ◆ **Deep draft: there is a local maximum**

## 3.2 Drag force in a two-layer fluid



Drag force with draft  $d=0.14m$  (a) and  $d=0.2m$  (b) vs. towing speed.  
 $h_1=0.2m$ ,  $h_2=0.4m$



- ①  $h=23cm$
- ②  $h=5cm$
- ③  $h=2.5cm$
- ④  $h_1=2cm$
- ⑤  $h_1=2cm$ , experiment data

(Ekman, 1904)

# 3.3 Dead water coefficient in a two-layer fluid

## ➤ Dead water resistance coefficient

$$F = \frac{1}{2} C \rho S V^2$$

$$C_d = C_{\text{two-layer}} - C_{\text{uniform}}$$

## ➤ $Fr$ in a two-layer fluid

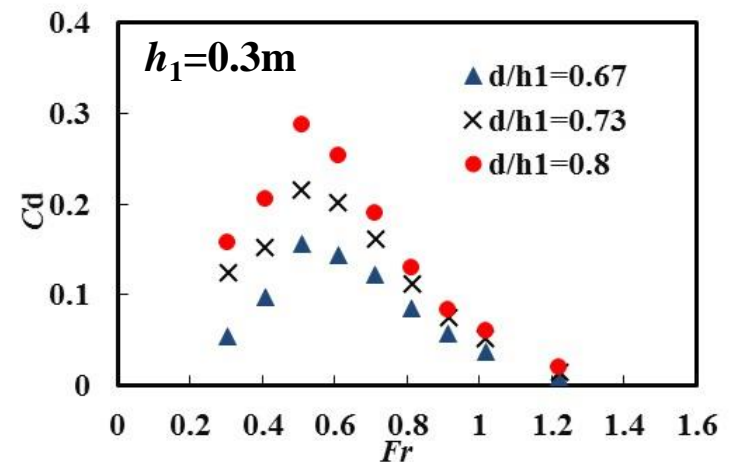
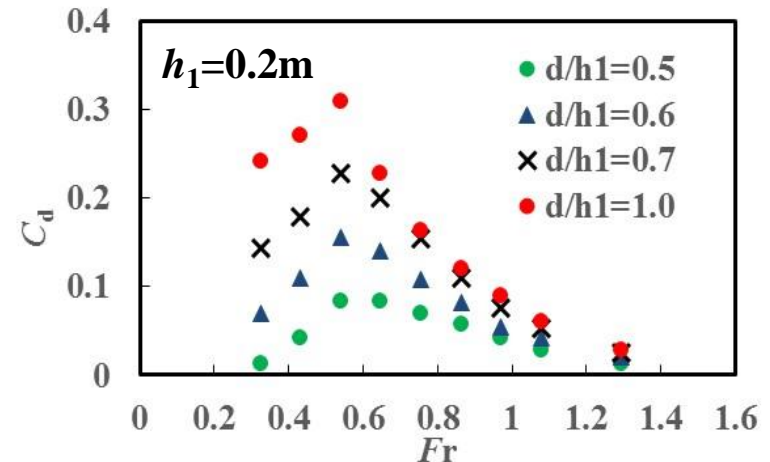
$$Fr = \frac{V}{c_0}$$

The maximum wave speed in two-layer fluid:

$$c^2 = \frac{g(\rho_2 - \rho_1)}{\rho_2} \frac{h_1 h_2}{h_1 + h_2}$$

$$h_1 = 0.2\text{m}, c_0 = 0.1785\text{m/s}$$

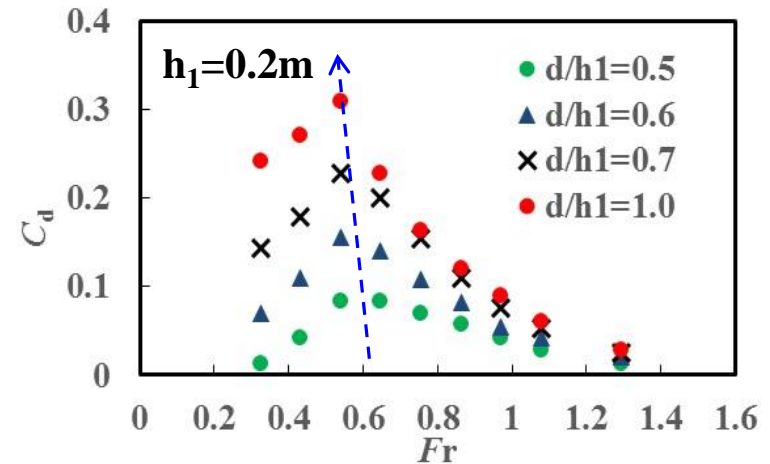
$$h_1 = 0.3\text{m}, c_0 = 0.1793\text{m/s}$$



Dead water resistance coefficient  $C_d$  vs.  $Fr$

# 3.3 Dead water coefficient in a two-layer fluid

- ◆  $C_d$  attains a maximum and the corresponding  $Fr$  down shifts slightly with the increase of draft.
- ◆ When  $C_d$  gets the maximum, the  $Fr$  is much smaller than the critical  $Fr$  1.0, about 0.5~0.6.



Added resistance coefficient  $C_{add}$  vs.  $Fr$

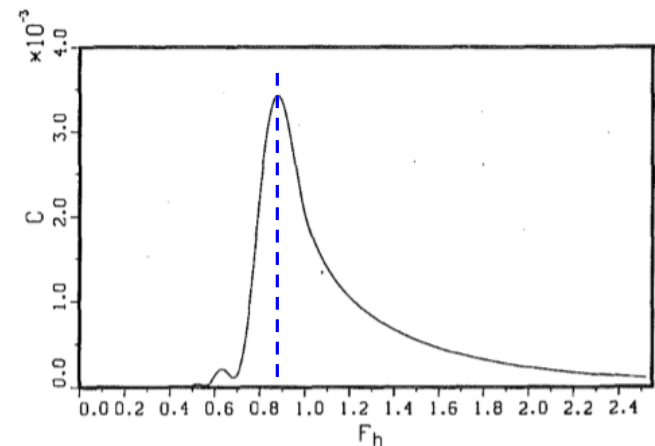
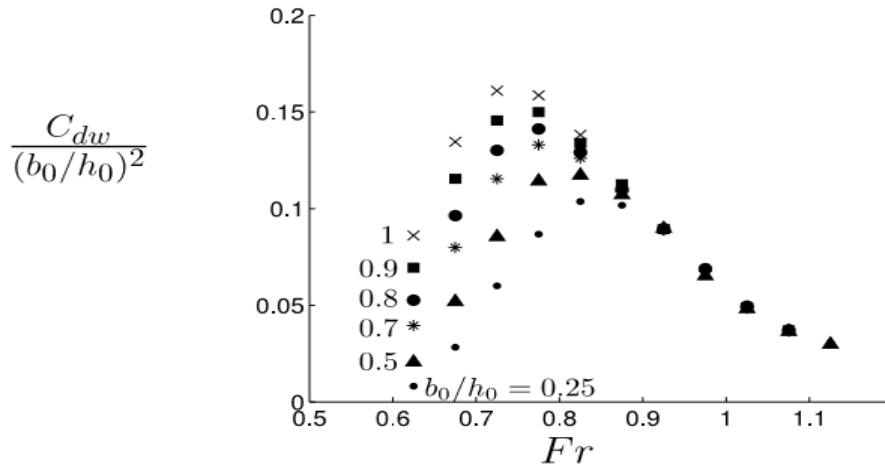


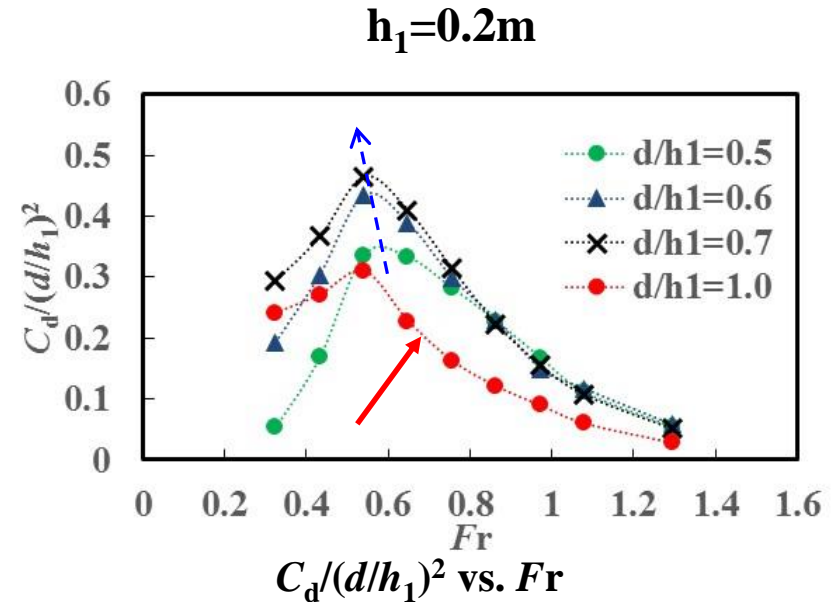
Fig. 1 Wave resistance coefficient  $C = 4R_w/\rho_1 U^2 DL$  of a prolate-spheroid of length  $L$  and maximum diameter  $D$  moving on the free-surface of a two-layer fluid:  $h_1 = h$ ,  $h_2 \rightarrow \infty$ ,  $D/h = 0.9$ ,  $L/h = 10.0$

# 3.3 Dead water coefficient in a two-layer fluid

$$C_d/(d/h_1)^2$$

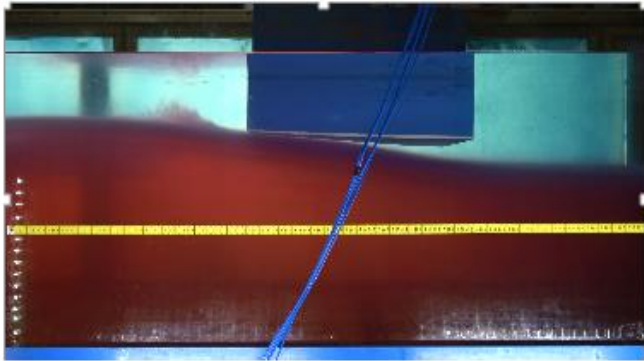


(J. Grue, 2015)

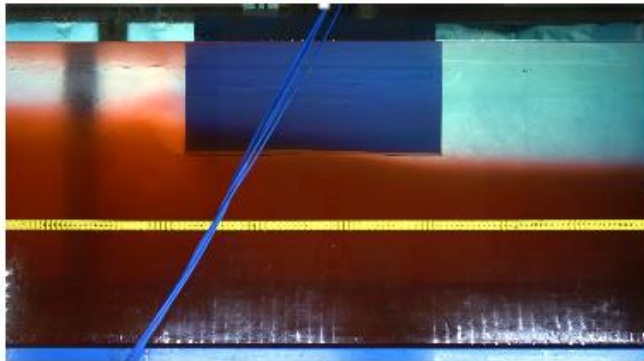


- ◆  $d/h_1=0.5\sim0.7$ :  $C_d/(d/h_1)^2$  depends on the Froude number only in the range close to critical speed ( $Fr > 0.85$  in the present), irrespective of the draft.
- ◆ The above conclusion is not suitable for the draft  $d/h_1=1.0$

# 3.3 Dead water coefficient in a two-layer fluid

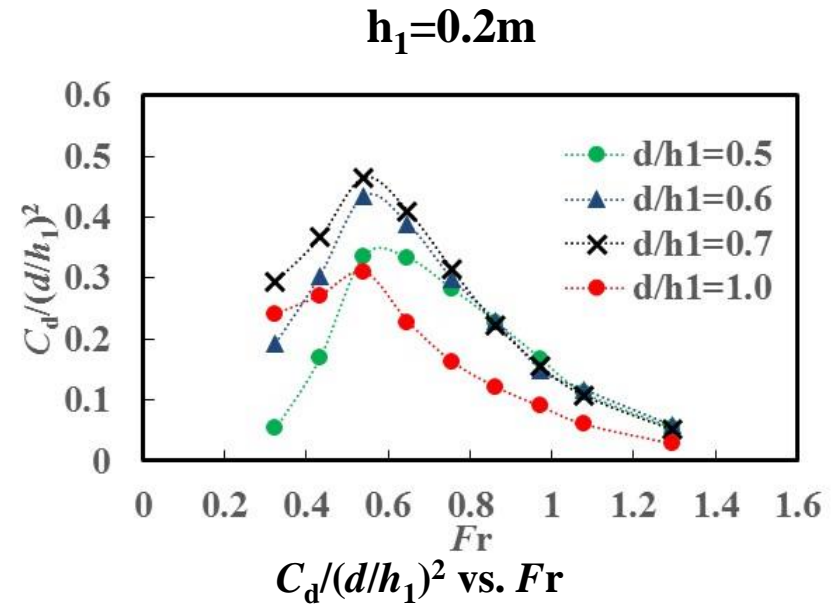


$d=0.14\text{m}$ ,  $d/h_1=0.7$



$d=0.2\text{m}$ ,  $d/h_1=1.0$

$V=0.12\text{m/s}$

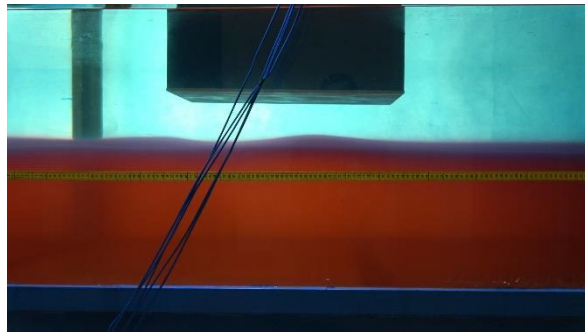


◆ Nonlinear effect

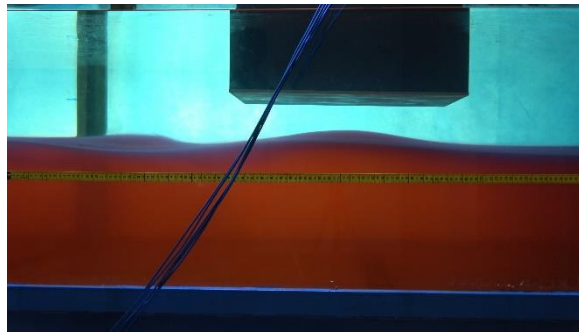
◆ Turbulent effect



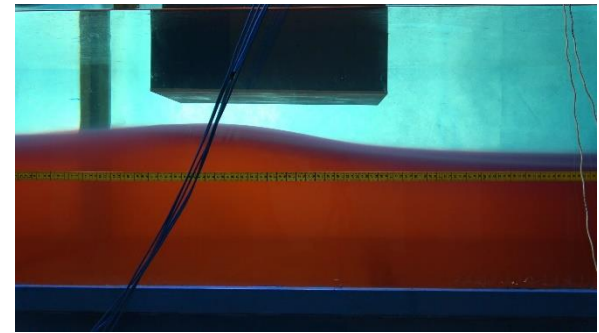
# 3.4 Pycnocline elevation



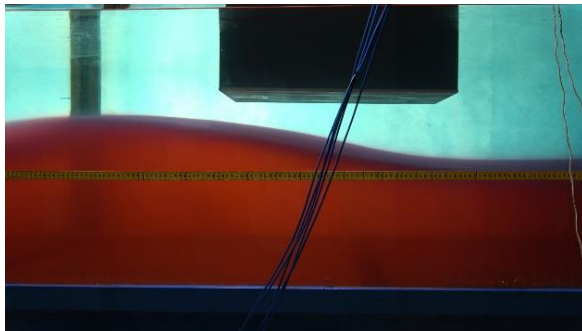
8cm/s



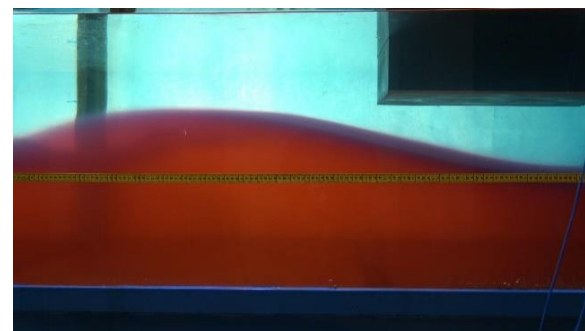
10cm/s



12cm/s



14cm/s



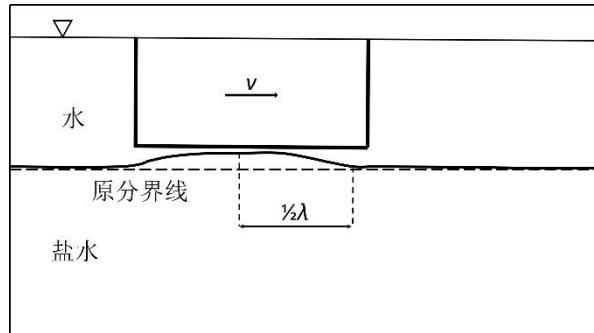
16cm/s

$d=10\text{cm}$ ,  $h_1=20\text{cm}$ ,  $d/h_1=0.5$

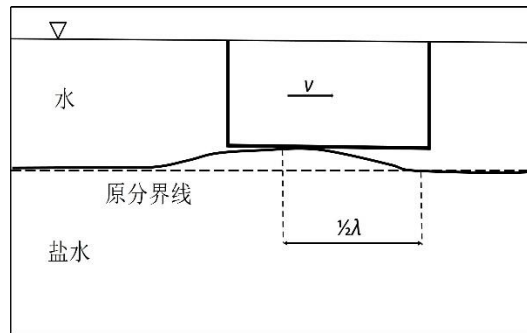
With the increase of towing velocity :

- ❑ Internal wave length becomes longer
- ❑ The position of internal wave crest is farther away from the box

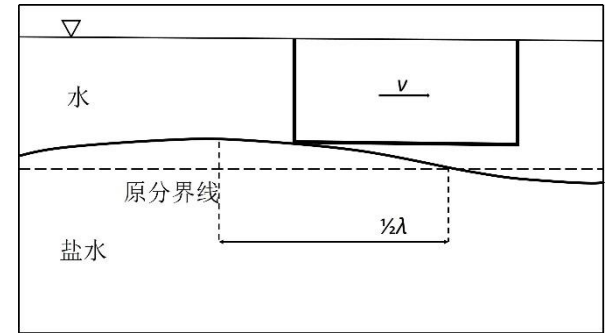
# 3.4 Pycnocline elevation



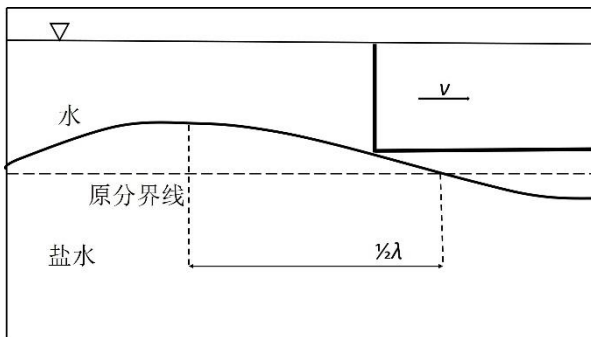
( a )  $v=8\text{cm/s}$



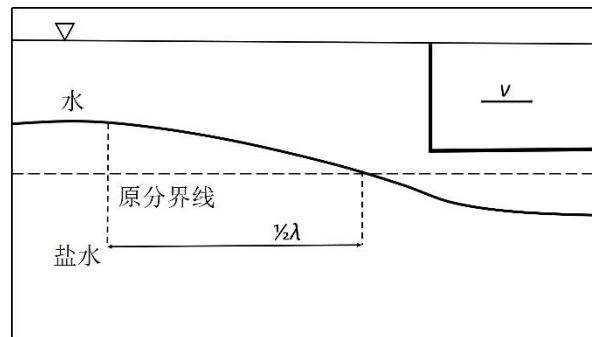
( b )  $v=10\text{cm/s}$



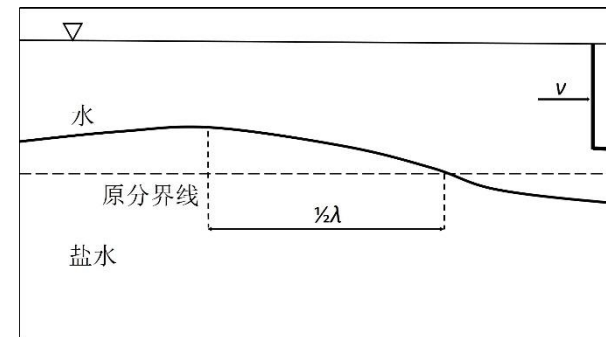
( c )  $v=12\text{cm/s}$



( d )  $v=14\text{cm/s}$



( e )  $v=18\text{cm/s}$



( f )  $v=24\text{cm/s}$

$$d=22\text{cm}, h_1=0.3\text{m}, d/h_1=0.73$$

# Conclusions

---

**Three-dimensional experiments are carried out to investigate the drag resistance on a barge model in a two-layer fluid.**

- ◆  $C_d$  attains a maximum and the corresponding  $Fr$  down-shifts slightly to smaller  $Fr$  with the increase of draft.
- ◆  $C_d$  reaches its maximum when the  $Fr$  in the range 0.5~0.6, much smaller than the critical  $Fr=1.0$ .
- ◆ For relative small drafts,  $C_d/(d/h_1)^2$  depends on  $Fr$  only in the range close to critical speed ( $Fr>0.85$ ), irrespective of the draft. But this conclusion is not suitable for the case  $d/h_1=1.0$  because of the nonlinear and turbulence effect.

---

***Thank you for your attention!***